# Sense of Number Visual Algebra Policy 



Graphic Design by Dave codirey Compilled by the Sense of Number Maths Teain For sole use within Sense of Number Primary School.

## "A pleture is worth 1000 wordst wanw-senseofinumber-coouk

# Guide to using $a$. Visual Algebra Policy 

The Sense of Number Visual Algebra Policy provides a visual interpretation of the progression required across the Primary school to help children meet the objectives found within Domain 10: Algebra in the new National Curriculum.

A school branded VAP is created by Dave Godfrey for individual schools when the school logo and school name are added to the footer of each slide.

Typical uses:
Classroom: The slides are printed out (e.g. A4) and the appropriate slides are displayed within each classroom for continual reference or on a working wall.
Teacher Reference: The slides are printed out (e.g. 9 slides per A4 page) and inserted in the teacher's planning folder.
Parents: The slides are used to communicate to parents the school"s approach to developing and teaching algebraic thinking.
Website: Selected slides from the VAP are inserted onto a school's maths webpages. (Please note: the VAP should not be made available for download.)

# Visual Algebra Policy 

1-4 Introduction Slides
5-8 General Algebra Slides

| Pages | Code |
| :--- | :--- |
| $9-14$ | AA |
| $15-23$ | AB |
| $24-31$ | AC |
| $32-37$ | AD |
| $38-56$ | AE |
| $57-69$ | AF |
| $70-73$ | AG |
| $74-92$ | AH |
| $93-98$ | AI |
| $99-103$ | AJ |

Years
FS=Y4
Y1-Y6
Y1-Y6
Y1-Y6 Abacus (patterns \& sequences)
Y1-Y6 Function Machines
Y4=Y6 Graphing Sequences
Y1=Y4 Balancing Stacks
Y1-Y6 Balancing Equations
Y4-Y6 Formulae
Y5-Y6 Algebra Word Problems

| Section | Y 1 | Y 2 | Y 3 | Y 4 | Y 5 | Y 6 |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
| A: PatterinS and Sequences | $9-11$ | $11-15$ |  |  |  |  |
| B: Counting Sequences | $15-16$ | $17-18$ |  | $19-21$ | $20-23$ |  |
| C: Number Shapes (P\&S) | 24 | 25 | 26,27 |  | $28-31$ |  |
| D: AbacuS (P\&S) | 32 |  | $33-35$ |  | 36,37 |  |
| E: Function Machines | 38 | $39-43$ | $44-47$ | $48-51$ | 52 | $53-56$ |
| F: Graphing SequenceS |  |  |  | 57,58 | $59-63$ | $61-69$ |
| G: Balancing Stacks | 70 | 70,71 | 72 | 73 |  |  |
| H: Balancing Equations | $74-76$ | 77,78 | 79 | 79,80 | $81-83$ | $84-92$ |
| I: Formulae |  |  |  | $93-95$ | $\mathbf{9 6 - 9 8}$ |  |
| J: Algebra Word Problems |  |  |  |  | $\mathbf{9 9 - 1 0 3}$ |  |

# Seeing a Sequence 

## A: Count



## B: Pattern

BBC BBG BBC B

## C: Terms of Sequence

labeling the position of the greens

## term

 county

|  |  | 1 |  |  | 2 |  |  | 3 |  |  |  |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 |  |  |
|  |  | 3 |  |  | 6 |  |  | 9 |  |  |  |

# Equals Sign is a Bollance 

## 四 <br> 

## Agebratic Notation


d $\div 2$

$d=2-d=2$


# Letters in Algebra 



| Number of Eggs | $e$ | 12 | 24 | 36 | $12 b$ |
| ---: | :---: | :---: | :---: | :---: | :---: |
| Number of Full Boxes | $b$ | 1 | 2 | 3 | $\frac{e}{12}$ |
|  |  |  |  |  |  |



In Algebra letters are variables!

AA: Pattems is Sequences


# AA: Potterns a Sequences 1 What are the missing terms? 


$5,10,15,20, \ldots, 45$,
$22,20, \ldots, 18,16, \ldots$,

## $30,40, \ldots, 60,70, \ldots$

# AA: Potterns \& Sequences 2a <br> <br> What are the missing terms? 

 <br> <br> What are the missing terms?}

$37,39, \ldots, 43,45, \ldots$

## 180, 170, _, 150, 140, _,

# AA: Patterns a Sequences 2b <br> What are the missing terms? 

## $1,4,-,-13,16,-,-$

## $5,9, \ldots, 17, \ldots, 25$,

## $36,42, \ldots, 54,60, \ldots$,

# AA: Potterns \& Sequences $3 \quad$ What are the missing terms? 




## 1, 5, 9, 13, —. —. —.,

# AA: Potterns a Sequences 3/4 <br> What are the missing terms? 

$12,8,4,0, \ldots, \ldots, 12$, $5,3,1, \ldots, \ldots,-5,=7$,

## $32,22,12,2, \ldots, \ldots$

$\underset{120}{\boldsymbol{1} 2} \mathbf{A}$ : Counting Sequences


# $\underset{12 b}{\mathrm{AB}}$ : Counting Sequences "Who is going to say 100?" 


$\underset{230}{A B}$ : Counting Sequences


# $\underset{2 / 3 b}{\mathbf{A B}}$ : Counting Sequences $\underset{\text { whoi is ging }}{ }$ 


$\underset{\substack{3 / 4}}{A B}$ : Counting Sequences


| 3 | 7 | 11 | 15 | 17 | 19 | $?$ |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |

$\underset{4 / 50}{4 B}$ : Counting Sequences

$\underset{4 / 55}{\text { AB: }}$ Counting Sequences


# AB: Counting Sequences 5/6 "Who is going to say 24 ?" 


"Who is
going to
say 39 ?


| $y=4 x-2$ |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $x$ | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 |
| y | 2 | 6 | 10 | 14 | 18 | 22 | ? | ? |


| $y=4 x-1$ |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 |
| $y$ | 3 | 7 | 11 | 15 | 17 | 19 | $?$ | $?$ |

# AC: Number Shapes Sequences 




# AC: Number Shapes 3a 






AC: Number Shapes

| $\mathbf{x}$ | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 |
| ---: | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| $\mathbf{y}$ | $\mathbf{1}$ | 5 | 9 | 13 | 17 | 21 | $?$ | $?$ |

20


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## AD: Abacus 1/2



| 1 | $\rightarrow$ | 3 |
| :--- | :--- | :--- |
| 2 | $\rightarrow$ | 6 |
| 3 | $\rightarrow$ | 9 |
| 4 | $\rightarrow$ | 12 |
| 5 | $\rightarrow$ | 15 |
| 6 | $\rightarrow$ | 18 |


| 3 |
| :--- |
| 6 |
| 9 |
| 12 |
| 15 |
| 18 |
| 2 |
| 2 |
|  |
|  |

$\underset{3 / 40}{ } \mathbf{A D}:$ Abacus $y=3 x$


| $x$ | $x 3$ | $y$ |
| :---: | :---: | :---: |
| 1 | $\rightarrow$ | 3 |
| 2 | $\rightarrow$ | 6 |
| 3 | $\rightarrow$ | 9 |
| 4 | $\rightarrow$ | 12 |
| 5 | $\rightarrow$ | 15 |
| 6 | $\rightarrow$ | 18 |

# AD: Abacus 

## $y=3 x$



## AD: Abacus 3/4c $y=3 x+1$

| $x$ | $x^{3}$ | $y$ | +1 | $y$ |
| :---: | :---: | :---: | :---: | :---: |
| 1 | $\rightarrow$ | 3 | $\rightarrow$ | 4 |
| 2 | $\rightarrow$ | 6 | $\rightarrow$ | 7 |
| 3 | $\rightarrow$ | 9 | $\rightarrow$ | 10 |
| 4 | $\rightarrow$ | 12 | $\rightarrow$ | 13 |
| 5 | $\rightarrow$ | 15 | $\rightarrow$ | 16 |
| 6 | $\rightarrow$ | 18 | $\rightarrow$ | 19 |




## AD: Abacus 5/6 <br> $y=3 x+1$

| $x$ | $x 3$ | $y$ | +1 | $y$ |
| :---: | :---: | :---: | :---: | :---: |
| 1 | $\rightarrow$ | 3 | $\longrightarrow$ | 4 |
| 2 | $\rightarrow$ | 6 | $\rightarrow$ | 7 |
| 3 | $\rightarrow$ | 9 | $\longrightarrow$ | 10 |
| 4 | $\rightarrow$ | 12 | $\rightarrow$ | 13 |
| 5 | $\rightarrow$ | 15 | $\rightarrow$ | 16 |
| 6 | $\rightarrow$ | 18 | $\longrightarrow$ | 19 |



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## AD: Abacus <br> 6



$$
y=2 x+7
$$

## AE: Doubling Machines



## ${ }_{22}$ AE: Doubling Machines



## AE: Function Machines 2b <br> Numerical Order



## AE: Function Machines 2c <br> Numerical Order



## AE: Function Machines 2d <br> Numerical Order



## AE: Function Machines 2e <br> Numerical Order



# AE: Function Machines 3a <br> <br> Numerical Order 

 <br> <br> Numerical Order}


# AE: Function Machines 3b 



# AE: Function Machines 3c <br> Random 



# AE: Function Machines 3d 



# AE: Function Machines 4a <br> Numerical Order 



| $x$ | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $x 4$ | 4 | 8 | 12 | 16 | 20 | 24 | 28 | 32 | 36 | 40 |
|  | 6 | 10 | 14 | 18 | 22 | 26 | 30 | 34 | 38 | 42 |
|  |  |  |  |  |  |  |  |  |  |  |

# AE: Function Machines 4b <br> Numerical Order 



# AE: Function Machines $4 c$ <br> Random 





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AE: Function Machines 2


# AE: Function Machines 

Guardian of the Rule

$\xrightarrow{\text { Maps onto }} \rightarrow$

# AE: Function Machines 

 6cGuardian of the Rule


# AE: Function Machines 

 6dGuardian of the Rule


$$
\begin{array}{ll}
\text { AF: Tines Tables sequenee } \\
\text { on © eraph }
\end{array}
$$

# AF: Terms of a Sequence 



First Term is
Step Size is
10th Term will be
100th Term will be $\qquad$

Hint:
Compare the sequence to the step size times-table


## AF: Graphing a Sequence

| g | $\times$ | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 7 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 12 | y | 12 | 8 | 4 | 0 | ? | ? | -12 | 12 |

Counting back in $\mathbf{4 ' s}^{\prime}$, starting at 12


## Each term moves on 2!

AF: Terms of a Sequence

| First |
| :--- |
| Term |
| Term |

# $\underset{56 f}{ } \mathbf{A F}$ : Negative Sequence 



Counting back in 2's, starting at 10

## $y=-2 x+12$



## AF: Graphing a Sequence

| y | $x$ | 1 | 2 | 3 | 4 |  |  | 6 | 7 |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 12 | y | 12 | 8 | 4 | 0 |  |  | ? | -12 |  |

Counting back in 4's, starting at 12 $y=-4 x+16$


AF: Connections 6d


| $x$ | 1 | 2 | 3 | 4 | 5 | 6 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| y | 3 | 6 | 9 | 12 | 15 | 18 |
| y + 2 | 5 | 8 | 11 | 14 |  |  |


| $x$ | $x 3$ | $y$ | +2 | $y$ |
| :---: | :---: | :---: | :---: | :---: |
| 1 | $\rightarrow$ | 3 | $\rightarrow$ | 5 |
| 2 | $\rightarrow$ | 6 | $\rightarrow$ | 8 |
| 3 | $\rightarrow$ | 9 | $\rightarrow$ | 11 |
| 4 | $\rightarrow$ | 12 | $\rightarrow$ | 14 |
| 5 | $\rightarrow$ | 15 | $\rightarrow$ | 17 |
| 6 | $\rightarrow$ | 18 | $\rightarrow$ | 20 |



$$
y=m x+c
$$

If m is $0, c$ is $\mathbb{1}: \mathrm{y}=1$
If $m$ is $\mathbb{1}, c$ is $\mathbb{1}: y \equiv x+1$
If $m$ is $2, c$ is $\mathbb{1}: y=2 x+1$
m = gradient
c = y intercept, when
$x$ is zero (zero term)


$$
y=m x+c
$$

If $m$ is $\mathbb{1}, c$ is $0: y \equiv x$
If $m$ is $\mathbb{1}, c$ is $\mathbb{1}: y \equiv x+1$
If $m$ is $1, c$ is $2: y=x+2$

```
m = gradient
c = y intercept, when
\(x\) is zero (zero term)
```


## AG: Balancing Stacks 1



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## AG: Balancing Stacks 1/2



## AG: Balancing Stacks 3



# AG: Balancing Stacks 4 



## AH: Balancing Equations 1a



## AH: Balancing Equations <br> 1b



## AH: Balancing Equations 1c



## $\underset{20}{\mathbf{A}} \mathbf{H}$ : Balancing Equations



## AH: Balancing Equations 2b


$\underset{64}{\text { AH: Balancing Linear Eqns. }}$


## AH: Balancing Equations



## AH: Balancing Equations 3/4



## AH: Balancing Equations 5a

## $(10 \times \triangle)+4=80=$



## AH: Balancing Equations 5b

## $(20 \times \triangle)+30=90=(10 \times \square)$



## AH: Balancing Equations 5c

## $5 n+10=58=n$



# AH: Balancing Linear Eqns. 6a <br> <br> Algebraic Notation 

 <br> <br> Algebraic Notation}

## $5 c \psi 4=4 c+12$ $-4$ 5c <br> $4 c$ C

$\underset{6 b}{\text { AH: Balancing Linear Eqns. }}$


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# AH: Balancing Linear Eqns. 

 $6 c$
## Algebraic Notation

$$
\begin{aligned}
& 5 x+6=22+x \\
&-x \\
& 4 x+6=22 \\
&-6=16 \\
& 4 x=64 \\
& \div 4=4
\end{aligned}
$$

AF: Balancing Linear Egins.


# AH: Balancing Linear Eqns. 

 $6 e$
## Algebraic Notation


$\underset{6 f}{\text { AH: Balancing Linear Eqns. }}$

## $3 n=4=2 n+3$



# AH: Balancing Linear Eqns. 6 g <br> <br> Algebraic Notation 

 <br> <br> Algebraic Notation}
$5 e=3$
+3
$=3 e+5$


Al: Formulae (Perimeter) 4a


# Al: Formulae (Perimeter) 4b <br>  




Al: Formulae (Area) | $b=$ bege |
| :---: |
| $h=h i j t$ |

5

## Area of a Rectangle

 $=b \times h$
$b=6 \mathrm{~cm}$
$\mathrm{h}=8 \mathrm{~cm}$
Area of a Triangle $=\frac{1}{2} \times b \times h$


Area $=0.5 \times 6 \mathrm{~cm} \times 8 \mathrm{~cm}=24 \mathrm{~cm}^{2}$
Area $=6 \mathrm{~cm} \times 8 \mathrm{~cm}=48 \mathrm{~cm}^{2}$

## Al: Formulae (General)

 5/6
$a+b$


# Al: The Pi ( $\pi$ ) you can't eat! 

6

$\Pi$ (Pi) is the ratio of a circle's circumference to it's diameter!
$\pi=\frac{\text { circumference }}{\text { diameter }}$

## Circumference $=\mathbf{3 . 1 4 1 5 9 2 6 5 3 5 9 0} \times$ Diameter

| diameter | diameter | diameter |  |
| :---: | :---: | :---: | :--- |
| $\mathbf{1}$ | $\mathbf{1}$ | $\mathbf{1}$ | $\mathbf{0 . 1 4 . .}$ |

Area of a Circle $=\pi x\left\|^{\prime \prime}\right\|^{\prime \prime}=\pi r^{2}$
Circumference of a Circle $=\mathbf{2} \pi r^{r}=\boldsymbol{\pi} d$

$$
\text { radius }=\frac{1}{2} \times \text { diameter }
$$



## AJ: Algebra Word Problems

 5/6aSuppose there are $y$ sheep on a bus. At a bus stop n more sheep get on the bus.

How many sheep are now on the bus?

## Answer: y + n



## AJ: Algebra Word Problems 5/6b

 A plece of wood is $\mathbf{2 5} \mathbf{c m}$ long.
## How much remains after II cut off a piece with length $x \mathrm{~cm}$ ?

Answer: 25 - x cm

$$
\frac{25 \mathrm{~cm}}{25-\mathrm{cm}}
$$

AJ: Algebra Word Problems 5/6c
A brick weighs w kg.
How much do six bricks weigh?
Answer: 6w


AJ: Algebra Word Problems 5/6d
A prize of $x$ is shared equally between you and four others.

## How much does each person recieve?



AJ: Algebra Problem Solving 5/6e 4 football teams werr in a lleague together", and played - each other once. How many fixtures were there?


Each team can't play themselves. Home and
Away fixtures for n
teams: $n x(n-\mathbb{D}) \equiv \mathbb{n}(n-\mathbb{D})$

## Pages in Bin!

AA: Counting Sequences
2/3+ "Who is going to say 30?

$\underset{v_{2}}{\mathbf{A B}}$ : Counting Sequences


## AE: Function Machines 3b



# AE: Function Machines 

 6Guardian of the Rule


# AE: Function Machines 



Here's the Guardian's Rule!


# AE: Function Machines 

Guardian of the Rule
$2 \xrightarrow{\text { Maps onto }} \sqrt{\text { Maps onto }} \sqrt{5} \xrightarrow{\text { Map }}$


## Here's the Guardian's Rule!



AG: Formulae (Area) \&

x


